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## G. VENKATASWAMY NAIDU COLLEGE (AUTONOMOUS), KOVILPATTI - 628 502.



## **UG DEGREE END SEMESTER EXAMINATIONS - APRIL 2025.**

(For those admitted in June 2024 and later)

## PROGRAMME AND BRANCH: B.Sc., STATISTICS

| SEM | CATEGORY   | COMPONENT          | COURSE CODE | COURSE TITLE               |
|-----|------------|--------------------|-------------|----------------------------|
| I   | PART - III | ELECTIVE GENERIC-1 | U24ST1A1    | MATHEMATICS FOR STATISTICS |

Date & Session: 26.04.2025/AN Time: 3 hours Maximum: 75 Marks Bloom's K-level Outcome Course Q. SECTION – A  $(10 \times 1 = 10 \text{ Marks})$ No. **Answer ALL Questions.** CO1 K1 In the decomposition of partial fractions, the denominator must be: a) A polynomial in its factored form b) A prime number c) A constant d) Any expression If P is of lower degree than  $Q, \frac{P}{Q}$  is called the \_\_\_\_\_ fraction. CO1 K2 2. c) simple d) none of the above b) improper a) proper CO2 K1 The value of e is. 3. a) 1.7183 b) 2.71828 c) 0.71828 d) 3 Which of the following is logarithmic series? CO2 K2 a)  $1 + \frac{x}{1!} + \frac{x^2}{2!} + \frac{x^3}{3!} + \cdots$ c)  $x - \frac{x^2}{2} + \frac{x^3}{3} - \cdots$ b)  $1 + x + x^2 + x^3 + \cdots$ d)  $x - \frac{x^2}{2!} + \frac{x^3}{3!} - \cdots$ If one root of the equation is 2+i then the other root is. K1 CO<sub>3</sub> b) 2-i c) -i d) 2 A polynomial equation of degree n has at most how many roots? CO3 K2 6. b) n+1 CO4 K1 A function that has only one output for every input is called: 7. a) Multi-valued function b) Single-valued function c) Inverse function d) Periodic function K2 The derivative of a constant function is always: CO<sub>4</sub> a) Zero b) One c) The same constant d) Undefined If there is no change in sign of f(x) when x is changed to -x, then function is CO<sub>5</sub> K1 9. called \_\_\_\_ function. a) odd b) periodic c) even d) implicit CO5 K2 10. The nth derivative of a function is obtained by: a) Differentiating the function once b) Integrating the function n times c) Differentiating the function n times d) Adding a constant to the function Bloom's K-level Outcome Course Q.  $\underline{SECTION - B} (5 X 5 = 25 Marks)$ No. Answer ALL Questions choosing either (a) or (b) CO1 КЗ 11a. Apply partial fractions method and split  $\frac{2x^2+3x+4}{(x-1)(x^2+2)}$ Compute  $\frac{x+4}{(x^2-4)(x+1)}$ CO1 К3 11b.

| CO2 | К3 | 12a. | Show that $\frac{\frac{1}{2!} + \frac{1}{4!} + \frac{1}{6!} + \dots}{\frac{1}{1!} + \frac{1}{3!} + \frac{1}{5!} + \dots} = \frac{e - 1}{e + 1}$ (OR) |
|-----|----|------|--|
| CO2 | КЗ | 12b. | Determine the proof of $\log x = \frac{x-1}{x+1} + \frac{1}{2} \frac{x^2-1}{(x+1)^2} + \frac{1}{3} \frac{x^3-1}{(x+1)^3} + \cdots$ .                 |
| CO3 | K4 | 13a. | Infer the roots of $x^4 + 2x^3 - 5x^2 + 6x + 2 = 0$ , given that 1+i is a root. <b>(OR)</b>  |
| CO3 | K4 | 13b. | If the roots of $x^3 + px^2 + qx + \lambda = 0$ are in G.P. Show that $\lambda p^3 = q^3$ .  |
| CO4 | K4 | 14a. | If $3x^2 - 7xy + 2y^2 + 2x - y + 3 = 0$ find y when $x = 3$ .  |
| CO4 | K4 | 14b. | Discover the maximum and minimum value of the function $f(x,y) = x^2y^2 - x^2 - y^2$ .   |
| CO5 | K5 |      | (OR)   |
| CO5 | K5 | 15b. | If $u = \frac{xy}{x+y}$ , show that $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = u$ .  |

| O                 | 70                 |           |  |
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| Course<br>Outcome | Bloom's<br>K-level | Q.<br>No. | $\frac{\text{SECTION} - C \text{ (5 X 8 = 40 Marks)}}{\text{Answer } \frac{\text{ALL}}{\text{Questions choosing either (a) or (b)}}$   |
| CO1               | КЗ                 | 16a.      | Construct $\frac{x}{(1+x^2)(3-2x)}$ into partial fractions. (OR)   |
| CO1               | К3                 | 16b.      | Prove that $\frac{1}{(1-ax)^2(1-bx)} = \frac{A}{(1-ax)^2} + \frac{AB}{1-ax} + \frac{B^2}{1-bx}$ if $\frac{1}{(1-ax)(1-bc)} = \frac{A}{1-ax} + \frac{B}{1-bx}$  |
| CO2               | K4                 | 17a.      | Sum the series $\frac{1}{10} + \frac{1.4}{10.20} + \frac{1.4.7}{10.20.30} + \cdots$  |
| CO2               | K4                 | 17b.      | Prove that $\log \sqrt{12} = 1 + (\frac{1}{2} + \frac{1}{3}) \frac{1}{4} + (\frac{1}{4} + \frac{1}{5}) \frac{1}{4^2} + (\frac{1}{6} + \frac{1}{7}) \frac{1}{4^3} + \cdots$                                   |
| CO3               | K4                 | 18a.      | If the roots are of $x^3 + px^2 + qx + r = 0$ are in A. P. Show that $2p^3 - 9pq + 27r = 0$ .  |
| CO3               | K4                 | 18b.      | Assuming $\alpha, \beta, \gamma$ are the roots of $x^3 + \alpha x^2 + bx + c = 0$ , find the equation whose roots are $\beta + \gamma - 2\alpha$ , $\gamma + \alpha - 2\beta$ , $\alpha + \beta - 2\gamma$ . |
| CO4               | K5                 | 19a.      | Differentiate $3x^5logx$ . (OR)  |
| CO4               | K5                 | 19b.      | Differentiate $\tan^{-1} \frac{\cos x}{1+\sin x}$ .  |
| CO5               | K5                 | 20a.      | Prove that $\frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = \sin 2u \text{ if } u = \tan^{-1} \left( \frac{x^3 + y^3}{x - y} \right).$ (OR)  |
| CO5               | K5                 | 20b.      | Find the maximum and minimum values of the function.<br>$f(x,y) = x^2y^2 - x^2 - y^2.$   |